## MDM4U - Unit 5 Probability Distributions

A. Identify the distribution type:

| 1. Number of attempts until you roll a 4 | Geometric |
| :---: | :---: |
| 2. 4 jellybeans are drawn without replacement. | Hypergeometric |
| 3. The probability of a bean germinating is 0.6 . At the same time, you plant 78 beans, one in each pot. | Binomial |
| 4. Waiting time before someone answers the phone | Geometric |
| 5. 8 people are chosen for a team. | Hypergeometric |
| 6. What is the probability you hit a red light $\mathbf{3}$ days in a row? | Binomial |
| 7. You roll 8 dice at the same time. | Binomial |
| 8. The heights of maple trees are normally distributed. | Normal |
| 9. 6 students form a committee. | Hypergeometric |
| 10. Let X be the number of times Tyler makes a basket during the $\mathbf{1 0}$ attempts. | Binomial |
| 11. Roll one regular 6 side dice. | Uniform |
| 12.Choose 2 adults to sit in 6 seats. | Hypergeometric |
| 13.Roll a pair of six-sided dice until you roll doubles" | Geometric |
| 14.The probability of the photocopier jamming is 0.8 . You want a probability distribution for 7 photocopies, one after another. | Binomial |
| 15.A family has 6 children. One parent has dimples, so the children have a probability of 0.4 of inheriting dimples. | Binomial |
| 16. One parent has dimples so the children have a probability Of 0.4 of inheriting dimples. How many children will they need to have until they have one with dimples? | Geometric |
| 17. You shuffle a card deck. Draw out eight cards without replacement and see how many hearts you have. | Hypergeometric |
| 18.Spin a spinner with 10 equal sections. | Uniform |
| 19. You shuffle a card deck. Draw out eight cards, replacing each one, and see how many hearts you have. | Binomial |
| 20. You are choosing $\mathbf{2}$ spotted kittens from a litter of 5 spotted and 6 non-spotted kittens. | Hypergeometric |
| 21. Let $X$ be the number of names Akhila draws until she draws an employee's name who does not have pierced ears. | Geometric |
| 22.Throw a dart at a dart board with 20 equal sections. | Uniform |
| 23. You have a 3-question multiple choice test with 5 options for each question. | Binomial |

## B. In a Binomial Distribution:

You have a 3-question multiple choice test, with 5 options for each question. What is the probability you get 2 right?

| 24.What is $X$ ? | The number of successes. <br> You get 2 questions right. |
| :--- | :--- |
| 25.What is $n$ ? | The number of trials. |
|  | There are 3 questions. |
| 26.What is $p$ ? | The probability of success. <br>  <br>  <br> $1 / 5$ probability of guessing correctly. <br> 27.What is $q$ ? <br> The probability of failure. <br> $4 / 5$ probability of guessing correctly. |

## C. In a Geometric Distribution:

Summer job selling by telephone. Nine out of ten hang up before they can give a sales pitch.

| 28.What is $x$ ? | The number of events until a success occurs. <br> The number of phone calls until can deliver sales pitch. |
| :--- | :--- |
| 29.What is $p$ ? | The probability of success. <br> $1 / 10$ people allow sales pitch. |
| 30.What is $q$ ? | The probability of failure. <br> $9 / 10 ~ p e o p l e ~ d o n ' t ~ a l l o w ~ s a l e s ~ p i t c h . ~$ |

## D. In a Hypergeometric Distribution:

Adults in the van. 10 adults, 8 children. 6 seats in van, 2 for adults.

| 31.What is $x$ ? | The number of successful things you want. <br> 2 adults will go in the van. |
| :--- | :--- |
| 32.What is $n$ ? | The total number of things to choose from. <br> 18 people in total. |
| 33. What is a? | The number of successful things to choose from. <br> 6 adults. |
| 34.What is $r$ ? | The total number of places to put things. <br> 6 seats in the van. |

## E. In a Uniform Distribution:

6 sides on the dice.

| 35.What is $n ?$ | How many of the equal section there are. <br> 6 sides |
| :--- | :--- |

## F. Convert the decimal to a percentage.

| 36. | 0.5 | $50 \%$ |
| :--- | :--- | :--- |
| 37. | 0.05 | $5 \%$ |
| 38. | 5 | $500 \%$ |
| 39. | 0.34 | $34 \%$ |
| 40. | 0.01 | $1 \%$ |
| 41. | 0.002 | $0.2 \%$ |
| 42. | 1 | $100 \%$ |

## G. Convert the percentage to a decimal.

| 43. | $10 \%$ | 0.1 |
| :--- | :--- | :--- |
| 44. $23 \%$ | 0.23 |  |
| 45. $5 \%$ | 0.05 |  |
| $46.100 \%$ | 1 |  |
| 47. $0.6 \%$ | 0.006 |  |

H. What is $\mathbf{q}$ ? (the probability of the opposite)

| 48. If $P$ is a percentage? | Subtract from 100 |
| :--- | :--- |
| 49. If $P$ is a decimal? | Subtract from 1 |
| 50. If $P$ is a fraction? | Subtract from 1 |
| 51. $p=20 \%$ | $q=80 \%$ |
| 52. $p=6 \%$ | $q=94 \%$ |
| 53. $p=97 \%$ | $q=3 \%$ |
| 54. $p=0.3$ | $q=0.7$ |
| 55. $p=0.49$ | $q=0.51$ |
| 56. $p=0.25$ | $q=0.75$ |
| 57. $p=0.01$ | $q=0.99$ |
| 58. $p=0.93$ | $q=0.07$ |
| 59. $p=1 / 12$ | $q=11 / 12$ |
| 60. $p=6 / 7$ | $q=1 / 7$ |
| 61. $p=3 / 4$ | $q=1 / 4$ |
| 62. $p=3 / 20$ | $q=17 / 20$ |

## I. Identify the term for each.

| 63.The calculation to answer: "how many red marbles will <br> you get on average?" | Expected Value |
| :--- | :--- |
| 64.Measure of spread in a probability distribution. | $\sigma$ |
| 65.Mound-shaped discrete probability distributions. | Binomial <br> Hypergeometric |
| 66.Mound-shaped continuous probability distribution. | Normal |
| 67.Left-skewed probability distribution. | None really <br> (maybe binomial with weird n and p) <br> Geometric |
| 68. Right-skewed probability distribution. | Expected Value |
| 69.Another term for the weighted mean. | Bernoulli |
| 70.A trial at the basis of the binomial distribution. | Expected Value |
| 71.Long-term average level of a random variable based on <br> its probability distribution | Discrete |
| 72.Discrete or continuous: Number of chairs. | Continuous |
| 73.Discrete or continuous: Temperature. | Continuous |
| 74.Discrete or continuous: Height of tree. | Discrete |
| 75.Discrete or continuous: Amount of students. | Expected Value |
| 76.The most likely the result of the next trial of a statistical |  |
| experiment. |  |$\quad$| Probability Distribution |
| :--- |
| 77.A mathematical function that describes the probability of |
| different possible values of a variable |$\quad$| Geometric |
| :--- |
| 78.The distribution type of the random bug walk. |
| 79.A use of the random bug walk. |
| Modelling sub-atomic particle <br> motion. |
| 80.First row of Pascal's triangle. |
| 81.Second row of Pascal's triangle. |
| 82.Third row of Pascal's triangle. |
| 83.Sum of the third row of pascal's triangle |
| 84.Formula for the nth row of pascal's triangle. |
| 85.Another term for a weighted average. |
| 86.All outcomes for a given process and their probabilities. |
| Probability Distribution |
| 2row-1 $=2^{\text {row-1 }}$ |

## J. Identify why each is important.

| 87.Expected Value | It is the most likely the result of the next trial of a statistical <br> experiment. |
| :--- | :--- |
| 88. Probability <br> Distributions | 1. Help us to understand the frequency of all outcomes of a <br> situation. <br> 2. They show which outcomes are more likely. <br> 3. We can use them to predict what to expect. <br> 4. Their Histograms allow us to visualize the probabilities of <br> all outcomes. |
| 89. Binomial Distribution | Models Bernoulii trials: <br> (a) Independent events. <br> (b) Each succeeds or fails <br> (c) With a specific probability |
| 90.Geometric <br> Distribution | Models probability of success after a specific number of failures. <br> Used to see how long you need to wait until something occurs. |
| 91.Hyper-Geometric <br> Distribution | Models the probability of success for a number of dependent <br> draws (or that occur without replacement). |
| 92.Uniform Distribution | Models a series of outcomes, all with equal probability. |
| 93. Random-walk <br> simulation | a. Used to model and understand complex physics. <br> b. Also models random events related to chaos theory <br> (weather, stock markets) |

## K. In the formula, what does each piece mean?

| 94.Binomial Distribution | $p=$ probability of a single event's success <br> $q=o p p o s i t e$ of $p$. probability of single event's failure. <br> $n=$ number of events <br> $x=$ the specific number of successes (eg $P(x=2)$... 2 red jellybeans) |
| :---: | :---: |
| 95.Geometric Distribution | $p=$ probability of a success on a single trial <br> $q=o p p o s i t e$ of $p$. probability of single event's failure. <br> $x=$ number of trials -1 . (eg. $P(x=0)$... first try) |
| 96. Hyper-Geometric Distribution | $\mathrm{n}=$ total number of things to choose from <br> $r=$ total number of places to put them <br> $a=$ number in the subgroup you are looking for <br> $x=$ specific number from the subgroup on this trial |
| 97.Uniform Distribution | $\min =$ lowest value you can roll. <br> max = highest value you can roll. <br> $\mathrm{n}=$ number of sides on the dice <br> note: x is not used in any formulas |

## L. Excel

| 98. How do you find $q$ ? | $=1-($ cell with $p)$ |
| :--- | :--- |
| 99. What is the formula for combinations? | $=\operatorname{combin}(\mathrm{A} 1, \mathrm{~B} 1)$ |
| 100. What is the symbol for exponents? | $\wedge$ |
| 101. What is the formula for square root? | $=\operatorname{sqrt(A1)}$ |
| 102. What is the formula for adding up <br> probabilities? | $=\operatorname{sum}(\mathrm{A} 1: \mathrm{A} 4)$ |
| 103. When do cells need the $\$ ?$ When they are the $\mathrm{p}, \mathrm{q}, \mathrm{n}, \mathrm{r}$ in the formula. <br> They don't change. <br>  X can't have the $\$$. It changes. <br> $\$$ is only used if the formula fills right |  |

