## EXERCISE 23B

1 Find $k$ in these probability distributions:

a | $x$ | 0 | 1 | 2 |
| :---: | :---: | :---: | :---: |
| $\mathrm{P}(X=x)$ | 0.3 | $k$ | 0.5 |

b

| $x$ | 0 | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{P}(X=x)$ | $k$ | $2 k$ | $3 k$ | $k$ |

2 The probabilities of Jason scoring home runs in each game during his baseball career are given in the following table. $X$ is the number of home runs per game.

| $x$ | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $P(x)$ | $a$ | 0.3333 | 0.1088 | 0.0084 | 0.0007 | 0.0000 |

a State the value of $P(2)$.
b What is the value of $a$ ? Explain what this number means.
c What is the value of $P(1)+P(2)+P(3)+P(4)+P(5)$ ? Explain what this means.
d Draw a probability distribution spike graph of $P(x)$ against $x$.

3 Explain why the following are not valid probability distribution functions:
a

| $x$ | 0 | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: | :---: |
| $P(x)$ | 0.2 | 0.3 | 0.4 | 0.2 |

b

| $x$ | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: |
| $P(x)$ | 0.3 | 0.4 | 0.5 | -0.2 |

4 Sally's number of hits in each softball match has the following probability distribution:

| $x$ | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{P}(X=x)$ | 0.07 | 0.14 | $k$ | 0.46 | 0.08 | 0.02 |

a State clearly what the random variable represents.
b Find $k$.
c Find: i $\mathrm{P}(X \geqslant 2)$
ii $\quad \mathrm{P}(1 \leqslant X \leqslant 3)$

## Answers:

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1 a $k=0.2 \quad$ b $k=\frac{1}{7}$
2 a $P(2)=0.1088$
b $a=0.5488$ is the probability that Jason does not hit a home run in a game.
c $P(1)+P(2)+P(3)+P(4)+P(5)=0.4512$ and is the probability that Jason will hit one or more home runs in a game.
d


3 a $\sum P\left(x_{i}\right)>1$ b $P(5)<0$ which is not possible
4 a $X$ is the number of hits that Sally has in each match.
$X=0,1,2,3,4$, or 5
b $k=0.23$
c i $\mathrm{P}(X \geqslant 2)=0.79 \quad$ ii $\mathrm{P}(1 \leqslant X \leqslant 3)=0.83$

