## Factorial Notation



## How can we find out how many things there are without counting them?



When the licence plates have 5
numerical digits how many were there?


## What about when it went up to 6 digits?



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Now, how many?



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Suppose that we have 1 thing. How many ways can it be arranged?

Suppose that we have 1 thing. How many ways can it be arranged?

A

Suppose that we have 2 things. How many ways can they be arranged?

Suppose that we have 2 things. How many ways can they be arranged?
AB
BA

Suppose that we have 2 things. How many ways can they be arranged?
AB
BA


Suppose that we have 3 things. How many ways can they be arranged?

Suppose that we have 3 things. How many ways can they be arranged?

## ABC ACB <br> BAC BCA CBA CAB

Suppose that we have 3 things. How many ways can they be arranged?

## ABC ACB <br> BAC BCA <br> CBA CAB



Suppose that we have 4 things. How many ways can they be arranged?

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ABCD ABDC ACBD ACDB ADCB ADBC BACD BADC BCAD BCDA BDCA BDAC CABD CBAD CADB CABD CDAB CDBA DABC DBAC DBAC DBCA DCAB DCBA

Suppose that we have 4 things. How many ways can they be arranged?
ABCD ABDC ACBD ACDB ADCB ADBC BACD BADC BCAD BCDA BDCA BDAC CABD CBAD CADB CABD CDAB CDBA DABC DBAC DBAC DBCA DCAB DCBA


A factorial is the product of an integer and all the integers below it.

$$
\begin{aligned}
& 1!=1=1 \\
& 2!=\quad 2=1 \times 2 \\
& 3!=6=1 \times 2 \times 3 \\
& 4!=24=1 \times 2 \times 3 \times 4 \\
& 5!=120=1 \times 2 \times 3 \times 4 \times 5
\end{aligned}
$$

|  | A b C | - |
| :---: | :---: | :---: |
| 1 | 0! = | 1 |
| 2 | $1!=$ | 1 |
| 3 | 2! = | 2 |
| 4 | 3! = | 6 |
| 5 | 4! = | 24 |
| 6 | $5!=$ | 120 |
| 7 | $6!=$ | 720 |
| 8 | 7! = | 5040 |
| 9 | $8!=$ | 40320 |
| 10 | 9! = | 362880 |
| 11 | 10! = | 3628800 |
| 12 | 11! = | 39916800 |
| 13 | 12 ! = | 479001600 |

- Factorials grow very quickly.
- This is why counting things by hand can be difficult.



Get it?

|  | A ${ }^{\text {B }}$ | B $C$ | D |
| :---: | :---: | :---: | :---: |
| 1 | $0!$ | ! = | 1 |
| 2 |  | ! = | 1 |
| 3 |  | ! = | 2 |
| 4 |  | ! = | 6 |
| 5 |  | ! = | 24 |
| 6 |  | ! = | 120 |
| 7 |  | $!=$ | 720 |
| 8 |  | $!=$ | 5040 |
| 9 |  | ! = | 40320 |
| 10 |  | ! $=$ | 362880 |
| 11 |  |  | 3628800 |
| 12 |  |  | 39916800 |
| 13 | 12 ! | ! $=$ | 479001600 |

How else can you express 5!

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## $5!=1 \times 2 \times 3 \times 4 \times 5$

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$$
\begin{aligned}
& 5!=1 \times 2 \times 3 \times 4 \times 5 \\
& 5!=4!\times 5
\end{aligned}
$$

## $5!=1 \times 2 \times 3 \times 4 \times 5$

## How else can you express 5!

$5!=1 \times 2 \times 3 \times 4 \times 5$
$5!=4!\times 5$

$$
\begin{aligned}
& 5!=1 \times 2 \times 3 \times 4 \times 5 \\
& 5!=3!\times 4 \times 5
\end{aligned}
$$

Write using factorials
$3 \times 4 \times 5 \times 6=$

## Write using factorials

## $3 \times 4 \times 5 \times 6=\frac{1 \times 2 \times 3 \times 4 \times 5 \times 6}{1 \times 2 \times 3}$

## Write using factorials

## $3 \times 4 \times 5 \times 6=\frac{1 \times 2 \times 3 \times 4 \times 5 \times 6}{1 \times 2 \times 3}$

$$
=\frac{6!}{3!}
$$

# Simplify, then evaluate 

$$
\frac{7!}{4!}
$$

## Simplify, then evaluate

$$
\frac{7!}{4!}=\frac{7 \times 6 \times 5 \times 4!}{4!}
$$

## Simplify, then evaluate

$$
\begin{aligned}
\frac{7!}{4!} & =\frac{7 \times 6 \times 5 \times 4!}{4!} \\
& =7 \times 6 \times 5
\end{aligned}
$$

## Simplify, then evaluate

$$
\begin{aligned}
\frac{7!}{4!} & =\frac{7 \times 6 \times 5 \times 4!}{4!} \\
& =7 \times 6 \times 5 \\
& =210
\end{aligned}
$$

You have 5 different numbers, how many ways can they be arranged?


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You have 5 numbers, how many ways can they be arranged?


You have 5 numbers, how many ways can they be arranged?
$5 \times 4 \times 3 \times 2 \times 11$
Number of ways
$=5 \times 4 \times 3 \times 2 \times 1$
$=5$ !

You have 5 numbers, how many ways can they be arranged?


Number of ways
$=5 \times 4 \times 3 \times 2 \times 1$
$=5$ !
$=120$

You have 10 different numbers, how many ways 4 unique digits be arranged on a licence plate?

The digits will not repeat in this example.


You have 10 different numbers, how many ways 4 unique digits be arranged on a licence plate?

## $10 \times 9 \times 8 \times 7$

## $10!$ <br> $10 \times 9 \times 8 \times 7=\frac{10!}{6!}$



You have 10 different numbers, how many ways 4 unique digits be arranged on a licence plate?

## $10 \times 9 \times 8 \times 7$

## $10!$ <br> $10 \times 9 \times 8 \times 7=\frac{10!}{6!}$ <br> $=5,040$ <br> 

