### 1.6 Independent and Mutually Exclusive

1. Classify each pair as dependent or independent events:

|  | First Event | Second Event |
| :--- | :--- | :--- |
| (a) | Attending a rock concert on <br> Tuesday night | Passing a final exam on the <br> following Wednesday morning. |
| (b) | Eating chocolate | Winning at checkers |
| (c) | Having blue eyes | Having poor hearing |
| (d) | Attending an employee training <br> session | Improving personal productivity |
| (e) | Graduating from university | Running a marathon |
| (f) | Going to a mall | Purchasing a new shirt |

2. Classify each pair of events as mutually exclusive or non-mutually exclusive:

|  | Event A | Event B |
| :--- | :--- | :--- |
| (a) | Randomly drawing a grey sock <br> from a drawer | Randomly drawing a wool sock <br> from a drawer |
| (b) | Randomly selecting a student <br> with brown eyes. | Randomly selecting a student on <br> the honour roll. |
| (c) | Having an even number of <br> students in your class. | Having an odd number of <br> students in your class. |
| (d) | Rolling a six with a die | Rolling a prime number with a <br> die |
| (e) | Your birthday falling on a <br> Saturday next year | Your birthday falling on a <br> weekend next year. |
| (f) | Getting an A on the next test | Passing the next test |
| (g) | Calm weather at noon <br> tomorrow | Stormy weather at noon <br> tomorrow |
| (h) | Sunny weather next week | Rainy weather next week |

3. The probability of $A$ is 0.2 and the probability of $B$ is 0.4 . What are the probabilities of each of the following events if $A$ and $B$ are independent and if they are mutually exclusive?

|  | A and B are independent | A and B are mutually exclusive |
| :--- | :--- | :--- |
| (a) $\mathrm{P}(\mathrm{A} \cap \mathrm{B})$ |  |  |
| (b) $\mathrm{P}\left(\mathrm{A}^{\prime}\right)$ |  |  |
| (c) $\mathrm{P}\left(\mathrm{A}^{\prime} \cap \mathrm{B}\right)$ |  |  |
| (d) $\mathrm{P}\left(\mathrm{A}^{\prime} \cap \mathrm{B}^{\prime}\right)$ |  |  |
| (e) $\mathrm{P}(\mathrm{A} \cup \mathrm{B})$ |  |  |
| (f) $\mathrm{P}\left(\mathrm{A}^{\prime} \cup \mathrm{B}\right)$ |  |  |
| (g) $\mathrm{P}\left(\mathrm{A}^{\prime} \cup \mathrm{B}^{\prime}\right)$ |  |  |

4. (a) What is $\mathrm{P}\left(\mathrm{A} \cap \mathrm{A}^{\prime}\right)$ ? Why?
(b) What is $\mathrm{P}\left(\mathrm{A} \cup \mathrm{A}^{\prime}\right)$ ? Why?

## Answers

1. a. dep b. indep c. indep d. dep e. indep f. dep 2. a. non b. non c. mutually d. mutually e. non f. non 3. indep a. 0.08 b. 0.8 c. 0.32 d. 0.48 e. 0.52 f. 0.8 g. 0.92 mutually exclusive a. 0.6 b. 0.8 c. 0.4 d. 0.4 e. 0.6 f. 0.8 g. 14 . a. 0 . can't be in both A and in A'. They are mutually exclusive. b. sample space. everything is either in A or A'.
